

A New Sufficient Condition for Ergodic Chaos with an Application to the Matsuyama–Solow Model of Cyclical Growth*

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Abstract

In economic studies, the condition of expansiveness and unimodality has been widely recognized to be useful in proving ergodic chaos, which is a complex behavior with desirable observability. In this paper, a less conservative sufficient condition is proposed. We employ the result by Lasota and Yorke that proves existence of invariant measures for a dynamical system with an expansive iterate. An application to an economic model is also examined. It will be demonstrated that ergodic chaos can take place in a much larger range of parameter values than was perceived.

*This paper is to be submitted for the 2010 Fall Meeting of Japanese Economic Association. Final revision: April 19, 2010.

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