On the existence of Pareto optimal matchings without transitivity

We consider whether there exists a Pareto optimal matching in the marriage problem where individual preferences are not transitive. First, we exemplify that there can be no Pareto optimal matching. Second, we show that there exists a Pareto optimal matching in a certain class of pure matching problems.