Heston-Type Stochastic Volatility with a Markov Switching Regime^{*}

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Abstract. We construct a Heston-type stochastic volatility model with a Markov switching regime for a stock option price. An analytic solution which contains a matrix ODE is obtained and numerically calculated. Our model is flexible enough to induce a wide variety of volatility surfaces wit both flat and steep smiles/smirks for the same parameter values but different regimes.

Keywords: Stochastic volatility, Markov switching.

JEL classification: G12, E32,

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